

# MONONOBE - OKABE AND COULOMB EQUATIONS

prepared by Geo-Struct Sparks, LLC www.geostructsparks.com

Mononobe-Okabe and Coulomb Equation  
Sign Convention and Geometry

ver 2011-11-20

Project: Retaining Wall Calc By: 11/15/2011  
 Proj. No.: 123456 Checked:  
 Case:

Metric or English Units (M/E)	E	M or E
<b>Coulomb or Rankine Analysis</b>	COULOMB ANALYSIS	
<b>STRUCTURE AND SLOPE GEOMETRY</b>		
Angle of Slope at Top of Wall from horizontal	26.56	$\beta$ , degrees 0.463559 radians
Back of wall angle (batter) from vertical	15	$\theta$ , degrees 0.261799
<b>SOIL STRENGTH AND PROPERTIES</b>		
Friction Angle	34	$\phi$ , degrees 0.593412
Pa rotation relative to normal to wall	15.0	$\delta$ , degrees 0.261799

EARTHQUAKE ACCELERATION		
EQ kh* Typ. use 1/2 of max horiz acceleration for active walls, 1.5 x max accel for tiedback or batter pile walls(AASHTO, 1998 Div 1A Sect 7.4.3A)	0.1	decimal g (Comment)
EQ kv, most design methods permit leaving kv as zero	0	decimal g 0.099669 $\psi$ , radians

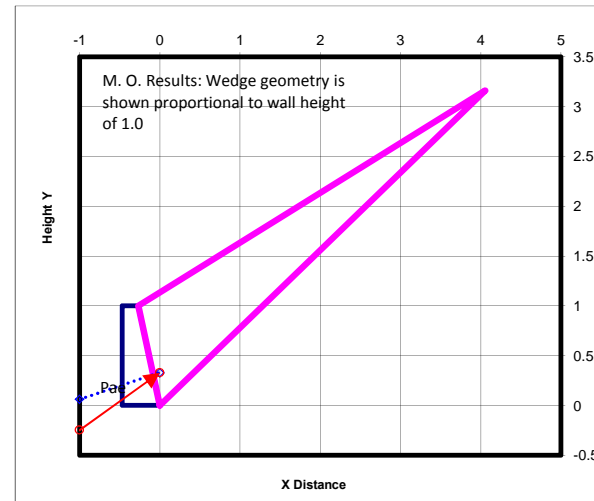
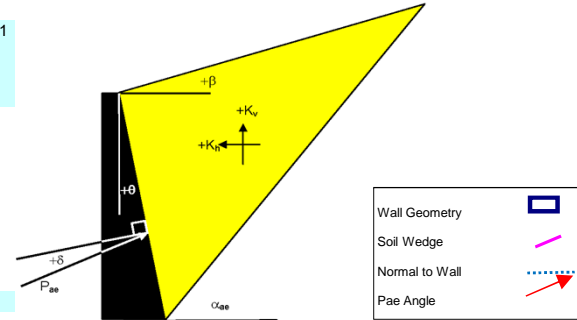
DISPLACEMENT BASED DESIGN		
Design peak acceleration for Site (> $k_i$ )	0.4	A, decimal g (actual A, not $k_i$ = 1/2 A typically used)
Design peak velocity, Normalized by A (FHWA value:)	760	V/A (mm/s) use 760 if not evaluating EQ records
Design peak velocity for Site	12.0	in/s

For information on input parameter selection, go to <http://www.geostructsparks.com/parameterguide.htm>

Franklin & Chang (1977) Estimate Upper Bound Residual Displacement: 11.1 inches

data from Newmark modeling from actual time histories -an approximation recommended by FHWA

$K_{ae} = \frac{\cos^2(\varphi - \theta)}{\cos^2(\theta) \cos(\delta + \theta) \left[ 1 + \frac{\sin(\varphi + \delta) \cdot \sin(\varphi - \beta)}{\cos(\delta + \theta) \cdot \cos(\beta - \theta)} \right]^2}$	Numerator	0.894005	
	Denominator	1.44953	0.62
$K_{ae} = \frac{\cos^2(\varphi - \psi - \theta)}{\cos(\psi) \cos^2(\theta) \cos(\delta + \theta + \psi) \left[ 1 + \frac{\sin(\varphi + \delta) \cdot \sin(\varphi - \psi - \beta)}{\cos(\delta + \theta + \psi) \cdot \cos(\beta - \theta)} \right]^2}$	Numerator	0.94716	
	Denominator	1.030514	0.92
$K_{pe} = \frac{\cos^2(\varphi + \theta)}{\cos^2(\theta) \cos(\delta - \theta) \left[ 1 - \frac{\sin(\varphi + \delta) \cdot \sin(\varphi + \beta)}{\cos(\delta - \theta) \cdot \cos(\beta - \theta)} \right]^2}$	Numerator	0.430413	
	Denominator	0.030545	14.09
$K_{pe} = \frac{\cos^2(\varphi - \psi + \theta)}{\cos(\psi) \cos^2(\theta) \cos(\delta - \theta + \psi) \left[ 1 - \frac{\sin(\varphi + \delta) \cdot \sin(\varphi - \psi + \beta)}{\cos(\delta - \theta + \psi) \cdot \cos(\beta - \theta)} \right]^2}$	Numerator	0.529838	
	Denominator	0.03859	13.73
$F_1 = \tan(\varphi - \psi - \beta)$	F1	0.030193	
$F_2 = \cot(\varphi - \psi - \theta)$	F2	4.233794	
$F_3 = \tan(\delta + \theta + \psi)$	F3	0.718853	
$\alpha_{ae} = (\varphi - \psi) + \text{atan} \left\{ \frac{\sqrt{F_1(F_1 + F_2)}(1 + F_3 F_2) - F_1}{1 + F_3(F_1 + F_2)} \right\}$		37.9	degrees



### References:

Kae and  $\alpha_{ae}$ : FHWA, 1998, Geotechnical Earthquake Engineering, FHWA-HI-99-012  
 Franklin A.G., and F.K. Chang, 1955, Earthquake Resistance of Earth and Rock-Fill Dams, Report 5: Permanent Displacement of Earth Embankments by Newmark Sliding Block Analysis, Misc. Paper 5-71-17, Soils and Pavements Laboratory, US Army Engineers Waterways Experiment Station, Vicksburg Mississippi.

Active Earth Pressure Coef., $K_{ae}$	0.92	Coulomb Ka (static)	0.62
$\Delta K_{ae}$	0.30		
Failure Angle $\alpha_{ae}$	37.9		
Kae Horizontal Compt	0.80		
Passive Earth Pressure Coef., $K_{pe}$	13.73	Coulomb Kp (static)	14.09

Unit Weight:	125	units:	pcf
$P_{ae}$	114.9	Pa	77.1
$\Delta P_{ae}$	37.8		
$P_{aeh}$	99.5		
$P_{pe}$	1716.2	Kp	1761.4